

Exercise 10.4 #62

Show that $\sum_{n=2}^{\infty} ((\ln n)^q / n^p)$ diverges for $-\infty < q < \infty$ and $0 < p < 1$.

(Hint: Limit Comparison with an appropriate p -series.)

In case $p=1$, you could solve the problem by The Integral Test.

(Hint: By Section 10.3 Exercise 55.)