

1. (a) Find  $\left. \frac{d \cos x^\circ}{dx} \right|_{x=60}$ . (b) Find  $\frac{dy}{dx}$  for  $y = \left[ \frac{1}{2}(1 - \cos(2t)) \right]^4$ .
2. Write down the definition for (a)  $\lim_{x \rightarrow -\infty} f(x) = \infty$ , (b)  $\lim_{x \rightarrow \infty} g(x) = 100$ .
3. For  $x \in \mathbb{R}$ , let  $f(x) = x^{6/11}$ . Prove that  $f'(0)$  does not exist.
4. Prove that the function  $\cos x$  is continuous on  $\mathbb{R}$ .
5. Let  $g$  be twice differentiable on  $(3, 10)$ . Prove that if  $g''(x) \neq 0$  for each  $x \in (3, 10)$ , then  $g$  has at most two zeros in  $(3, 10)$ .
6. Given  $\cos(x + 2y) = 0$ , use implicit differentiation to obtain  $dy/dx$  in terms of  $x$  and  $y$  and evaluate  $dy/dx$  at  $(\pi/6, \pi/6)$ .
7. Suppose that  $f$  is continuous on  $[\alpha, \beta]$  and  $f(\alpha) = f(\beta)$ . Prove that  $f$  has at least one critical number in  $(\alpha, \beta)$ .
8. Sketch the graph of  $f(x) = x + \frac{1}{x}$  for  $x \in \mathbb{R} \setminus \{0\}$  and find all asymptotes.
9. Let  $P$  be a point that is in the first quadrant and on the line  $4x + 3y = 12$ . Find the coordinates of  $P$  that maximize the area of the rectangle with vertices at the origin and  $P$  whose sides are parallel to the  $x$  and  $y$  axes.